

Answers for Worksheet 1

$m = 3$ 1) $m_{\perp} = -\frac{1}{3}$	2) $m = -\frac{1}{3}$ $m_{\perp} = 3$	3) slope = und $m_{\perp} = 0$	4) $x = 3$ $y = 2$	5) $x = 0$ $y = -\sqrt{2}$	6) $x = -\pi$ $y = \frac{\pi}{4}$
7) $y - 2 = 1(x - 1)$	8) $y - 0 = -2(x + 4)$	9) $y - \pi = \frac{\sqrt{2}}{2}(x + \pi)$	10) $y - 3 = \frac{3}{2}(x - 2)$	11) $y - \frac{3}{4} = \frac{11}{2}(x - 0)$	12) $y + 2 = 0(x - 3)$ or $y = -2$
13) $m = -\frac{3}{4}$ (4,0) (0,3)	14) $m = -\frac{4}{3}$ (3,0) (0,4)	15) undefined (4,0) none	16) $y - 2 = -2(x + 2)$ $y - 2 = \frac{1}{2}(x + 2)$	17) $y - 4 = -\frac{3}{4}(x + 6)$ $y - 4 = \frac{4}{3}(x + 6)$	18) $y = \frac{1}{2}$ $x = -1$
19) $\frac{67}{2}$	20) -13	21) -1	22) -6	23) a) $k = 2$ b) $k = -2$	

Answers for Worksheet 2

1) a) $f(0) = 3$ b) $f(\sqrt{3}) = 0$ c) $f(-2) = -1$	2) a) $f\left(-\frac{\pi}{4}\right) = \frac{\sqrt{2}}{2}$ b) $f(0) = 1$ c) $f(1) = 2$ d) $f(a^2) = 2a^2$	3) a) $f(x+h) = x^2 + 2xh + h^2 - 3x - 3h + 2$ b) $f(x+h) - f(x) = 2xh + h^2 - 3h$ c) $\frac{f(x+h) - f(x)}{h} = 2x + h - 3$
4) a) $f(g(2)) = 0$ b) $g(f(0)) = 0$ c) $g\left(f\left(\frac{\pi}{4}\right)\right) = \frac{\pi\sqrt{2}}{2}$	5) a) $f(g(x)) = \sqrt{2x+2}$ b) $g(f(x)) = 2\sqrt{x+2}$ c) $f(f(x)) = \sqrt{\sqrt{x+2}+2}$ d) $g(g(x)) = 4x$	6) a) $f(-2) = -2$ b) $f(0) = 2$ c) $f(1) = 3$ d) $f(s^2 + 2) = 2s^4 + 8s^2 + 10$
7) a) $D: x \geq 1$ or $[1, \infty)$ b) $D: \mathbb{R}$ or $(-\infty, \infty)$ c) $D: x \neq 2$ or $(-\infty, 2) \cup (2, \infty)$ d) $D: x \neq -1, -4$ or $(-\infty, -1) \cup (-1, 4) \cup (4, \infty)$		

Answers for Worksheet 3

- 1) a) $f(0) = 3$
 $f(8) = -2$ b) $f(-5) < 0$ since $(-5, f(-5))$ sits below the x-axis on the graph of $f(x)$.

c) $f(x) = 0$ @ $x = -3, 6, 10$ d) $f(x) = 3$ @ $x = 0, 4$

- e) $f(x)$ is increasing on $(-6, 2) \neq (8, 11)$ b/c the slope of $f(x)$ is positive

f) $f(x) = \frac{1}{2}$ three times g) $f(f(2)) = f(4) = 3$

h) $(-5, -2)$ $(11, 1)$

$$m = \frac{3}{16}$$

$$y + 2 = \frac{3}{16}(x + 5)$$

or

$$y - 1 = \frac{3}{16}(x - 11)$$

2) a) $f(0) = 1$
 $f(3) = 2$

b) $f(8) < 0$ since $(8, f(8))$ lies below the x-axis

c) $f(x) = 0$ @ $x = -1, 5, 9$ d) $f(x) = 2$ @ $x = 1, 3$

- e) $f(x)$ is decreasing on $(-3, -2), (2, 7)$ b/c the slope of $f(x)$ is negative

f) $f(x) = \frac{1}{4}$ three times

g) $m = \frac{f(5) - f(2)}{5 - 2}$

$$= \frac{0 - 3}{3}$$

$$= -1$$

h) $m = 0$

$$3) a) (f \circ g)(3) = f(g(3)) \\ = f(-1) \\ = 4$$

$$b) g(f(2)) = g(1) \\ = -2$$

$$c) g(f(5)) = g(-5) \\ = \emptyset$$

$$d) f(g(-3)) = f(-2) \\ = 3$$

$$e) g(f(-1)) = g(4) \\ = 2$$

$$f) f(g(-1)) = f(4) \\ = -\frac{7}{2}$$

4) a) At $t = 10$ min, Holly was 0.75 miles from home.

b) At ~ 14 min, Holly was 1 mile from home.

c) Holly was more than $\frac{1}{2}$ mile from home on $(7, 84)$.

d) Holly was resting on $(60, 74)$

e) Holly reached the ocean at $t \approx 38$ min, 2.5 miles from home

$$f) m = \frac{1.5}{20} = 0.075 \frac{\text{miles}}{\text{min}}$$

$$g) m = 0 \frac{\text{miles}}{\text{min}}$$

h) $t = 90$ min Holly returned home.

i) Holly was jogging fastest @ $t = 29$ min since the graph of her distance is steepest.

Answers to Worksheet 4

1)

$$a) f(4) = 103.3549$$

$$b) f(2.85) = 41.3678$$

$$c) f\left(\frac{7}{6}\right) = 2.0106$$

2)

$$b) f(-1.5) = 30.815$$

$$c) f(x) = 0 \text{ @ } x = -3.7519$$

$$x = 0.2035$$

$$x = 6.5484$$

$$d) f(x) \text{ has a max @ } (-2, 33)$$

$$e) f(x) \text{ has a min @ } (4, -75)$$

$$f) f(0) = 5$$

$$g) f(x) = g(x) \text{ @ } x = -3.4856$$

$$x = 1.861$$

$$x = 4.6245$$

3)

$$f(x) = 0 \text{ @ } x = -0.8767$$

$$x = 0$$

$$g(x) = -3 + e^{2x}$$

$$g(x) = 0 \text{ @ } x = 0.5493$$

$$h(x) = -3 + \ln x$$

$$h(x) = 0 \text{ @ } x = 20.0855$$

4)

$$a) f(x) = g(x) \text{ @ } x = 1.4645$$

$$b) f(x) = g(x) \text{ @ } x = -1.4168$$

$$x = 4.665$$

5)

$$f(x) \text{ has a max @ } (-0.458, -0.726)$$

$$(3.733, 10.216)$$

$$f(x) \text{ has a min @ } (0.910, -1.7307)$$

Answers to Worksheet 5

1) $x = \frac{3}{2}, x = -4$	2) $x = \frac{-1 + \ln 3}{2}$	3) $x = \frac{\pi}{18}, \frac{5\pi}{18}, \frac{13\pi}{18}, \frac{17\pi}{18}, \frac{25\pi}{18}, \frac{29\pi}{18}$
4) $x = 4 + e^{-6}$	5) $x = -1.6729, 1.469, 0.203$	6) $x = -0.287, 0.957$
7) (1,1)	8) (2,2), (-1,5)	9) (-1,0), (0,1), (1,0)
10) (1,5), (3,3)	11) (-2.057, -0.884), (2.638, 0.481)	

Answers to Unit 1 Review

1. $y + 6 = 3(x - 1)$	2. $x = 0$	3. $y - 3 = -\frac{2}{5}(x - 3)$ or $y - 5 = -\frac{2}{5}(x + 2)$	4. $y + 12 = -\frac{4}{3}(x - 4)$
5. $y - 2 = \frac{2}{3}(x + 1)$	6. a) $f(-3) = 18$ b) $f(a + 2) = a^2 - a - 12$ c) $\frac{f(x + h) - f(x)}{h} = 2x + h - 5$	7. a) $f(-3) = 1$ b) $f(-1) = -1$ c) $f(1) = \emptyset$ d) $f(b^2 + 2) = -b^2$	8. (-2,0), (1,0)
9. $x = \frac{\ln 20}{5}$	10. $x = \frac{\pi}{12}, \frac{5\pi}{12}, \frac{13\pi}{12}, \frac{17\pi}{12}$	11. $f(-2) = 6; f(-8) = -4$	
12. $f(x) = 0$ at $x = -10, -5, 0$, and 5		13. $f(x) > 0$ on $(-\infty, -10), (-5, 0), (0, 5), (5, \infty)$	
14. $f(x) = 1$ six times		15. $f(x)$ is increasing on $(-8, -2), (0, 2)$, and $(5, \infty)$	
16. $f(-4) > 0$			